

6<sup>a</sup> Escola de Astrofísica e Gravitação  
IST, Lisboa, 4 – 8 Sep 2012

# A brief introduction to the AdS/CFT conjecture

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# AdS/CFT: what is it about?

AdS = anti-de Sitter spacetime

(maximally symmetric solution of the Einstein equations with a negative cosmological constant)

CFT = conformal field theory

(relativistic quantum field theory invariant under scaling transformations)



# AdS/CFT: what is it about?

- It is a conjectured mapping between two (apparently) completely different theories:



- Holographic in nature ('CFT lives at the boundary of AdS')
- It is a powerful correspondence (strong-weak duality).
- Can extend to situations  $\neq$  CFTs ('gauge/gravity correspondence').

# Vast literature

- Polchinski's books "String Theory" (1998)
- Johnson's book "D-branes" (2003)
- Aharony, Gubser, Maldacena, Ooguri & Oz (AGMOO's) review "Large N field theories, string theory and gravity", hep-th/9905111
- D'Hoker & Freedman's TASI lectures "Supersymmetric gauge theories and the AdS/CFT correspondence", hep-th/0201253
- ➔ ○ Mateos' review "String Theory and Quantum Chromodynamics", arXiv:0709.1523 [hep-th]
- Nastase's review "Introduction to AdS-CFT", arXiv:0712.0689 [hep-th]
- Gubser & Karch's review, "From gauge-string duality to strong interactions: A Pedestrian's Guide", arXiv:0901.0935 [hep-th]
- ➔ ○ McGreevy's review, "Holographic duality with a view toward many-body physics", arxiv:0909.0518 [hep-th]
- ➔ ○ Argyres' lecture, "Introduction to the AdS/CFT correspondence" in "From gravity to thermal gauge theories: the AdS/CFT correspondence", ed. Papanthopoulos (2011)



# Impact of AdS/CFT on High Energy Physics



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# AdS/CFT: not so crazy...

- A quantum theory of gravity should contain a spin-2 massless particle ('graviton'). The Weinberg-Witten theorem forbids such particles in QFTs with usual stress tensors.

➔ The graviton and the CFT should live on different spaces.

- The Holographic Principle implies that the quantum theory of gravity must have a number of degrees of freedom which scales like the area, not the volume.

➔ The quantum gravity theory should live in one more dimension than the CFT.

- It is convenient to slice up QFTs according to energy scale  $u$ .  
The Renormalization Group Equations tell us how coupling constants depend on  $u$ .

➔ The extra dimension should be identified with energy scale.

# AdS = anti-de Sitter spacetime

○ In vacuum: 
$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} + \Lambda g_{\mu\nu} = 8\pi T_{\mu\nu} = 0$$

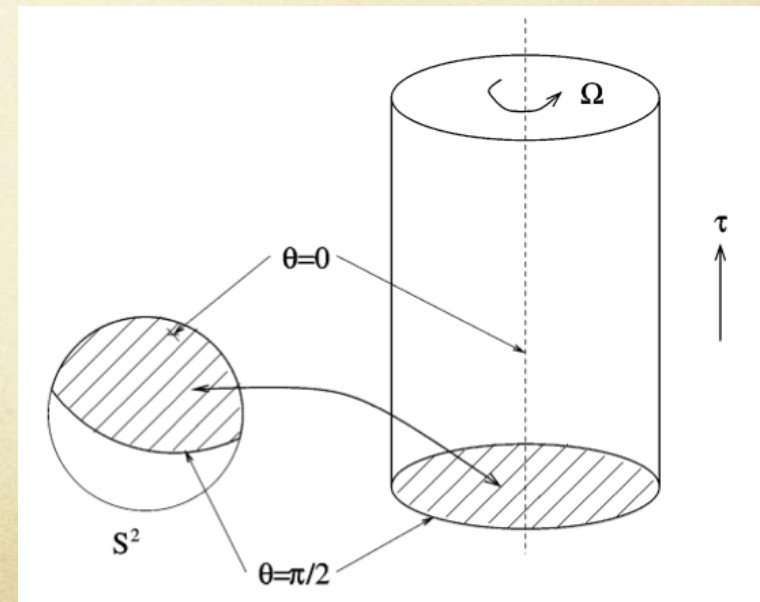
○ Maximally symmetric  $\rightarrow$  constant curvature: 
$$R = \frac{2d}{d-2}\Lambda$$

○ Global parametrization: 
$$ds^2 = -R^2 \cosh^2\left(\frac{\rho}{R}\right) dt^2 + d\rho^2 + R^2 \sinh^2\left(\frac{\rho}{R}\right) d\Omega_{d-2}^2$$

○ Boundary at  $\rho = \infty$  with topology  $\mathbb{R} \times S^{d-2}$ .

○ Another parametrization (not global):

$$ds^2 = \frac{R^2}{r^2} dr^2 + \frac{r^2}{R^2} (-dt^2 + d\bar{x}^2)$$

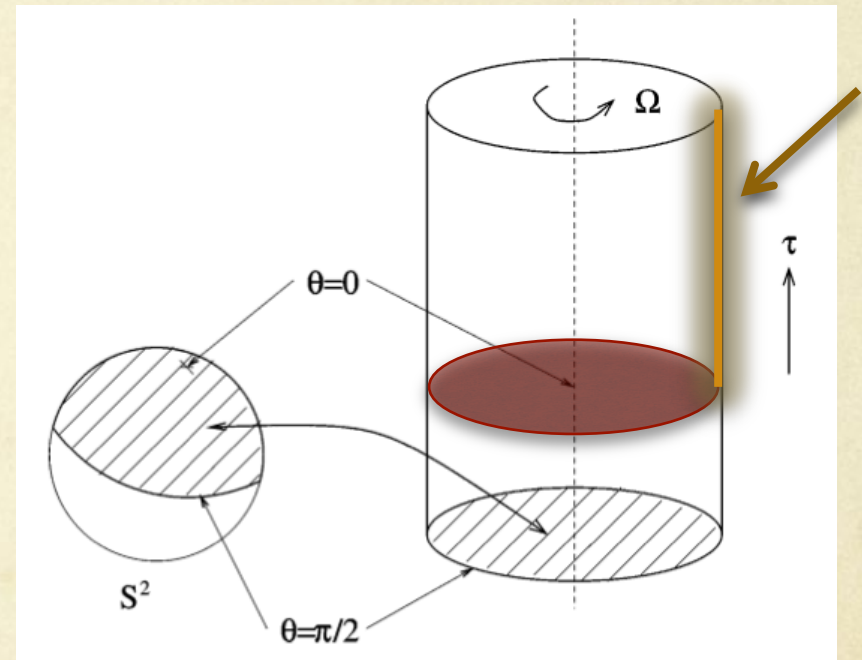
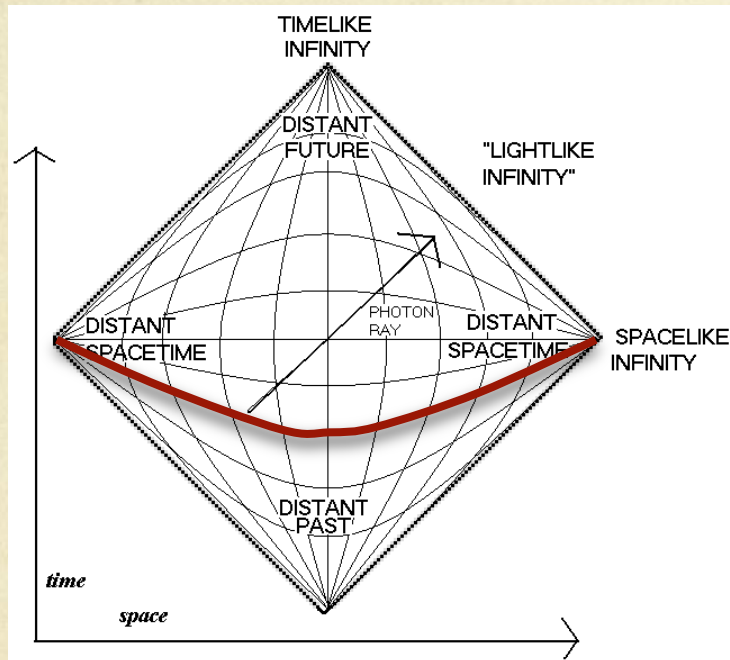




# AdS vs Minkowski

- Minkowski is the maximally symmetric solution of Einstein eqs with  $\Lambda=0$ :

$$ds^2 = -dt^2 + d\vec{x}^2 = -dt^2 + dr^2 + r^2 d\Omega_{d-2}^2$$



- Minkowski is globally hyperbolic but AdS is not.  
Data must be specified on the boundary of AdS.

# CFT = conformal field theory

- Quantum field theory (QFT) is the framework for constructing quantum mechanical models of systems classically represented by an infinite number of degrees of freedom (fields).
- Example: the standard model of particle physics.
- Unitary scale invariant QFTs are also conformally invariant.

conformal group  $\left\{ \begin{array}{ll} M_{\mu\nu} & \text{Lorentz rotations} \\ P_{\mu} & \text{Translations} \\ D & \text{Dilatations} \\ K_{\mu} & \text{Special conformal transformations} \end{array} \right.$



# CFT local operators and correlators

conformal group  $\left\{ \begin{array}{ll} M_{\mu\nu} & \text{Lorentz rotations} \\ P_{\mu} & \text{Translations} \\ D & \text{Dilatations} \\ K_{\mu} & \text{Special conformal transformations} \end{array} \right.$

- Generators satisfy an algebra which is  $SO(d,2) \supset SO(d) \times SO(2)$ .

spin  $\nearrow$  conformal dimension  $\Delta$

Classify local operators by their transformation properties under  $SO(d) \times SO(2)$ .

$$O_{\Delta}(\lambda x^{\mu}) = \lambda^{-\Delta} O_{\Delta}(x^{\mu})$$

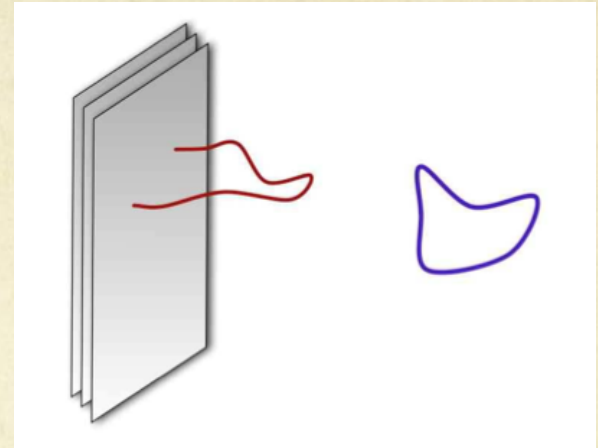
- Correlation functions are highly constrained by conformal symmetry:

$$\langle O_{\Delta_1}(x_1) O_{\Delta_2}(x_2) \rangle = \frac{\delta_{\Delta_1, \Delta_2}}{|x_1 - x_2|^{2\Delta_1}}$$

# Recap: string theory basics

- ST is a theory of strings, but not only!

It is inhabited by other creatures and among the most important are D-branes.



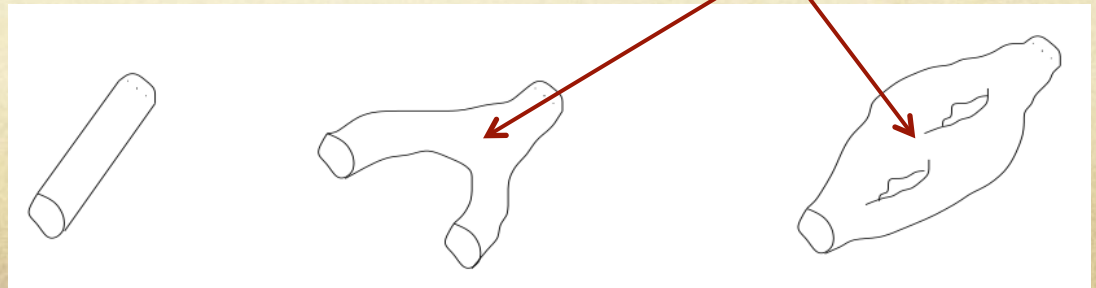
- What parameters do we have in ST?

➔  $\alpha'$  controls stringy effects. String tension is  $T = \frac{1}{2\pi\alpha'}$

➔  $g_s$  controls quantum effects. ('string coupling constant')

➔ Splitting/joining of closed (open) introduces a factor of  $g_c$  ( $g_o$ )

$$g_o^2 \sim g_c = g_s \alpha'^2$$





# Recap: D-branes

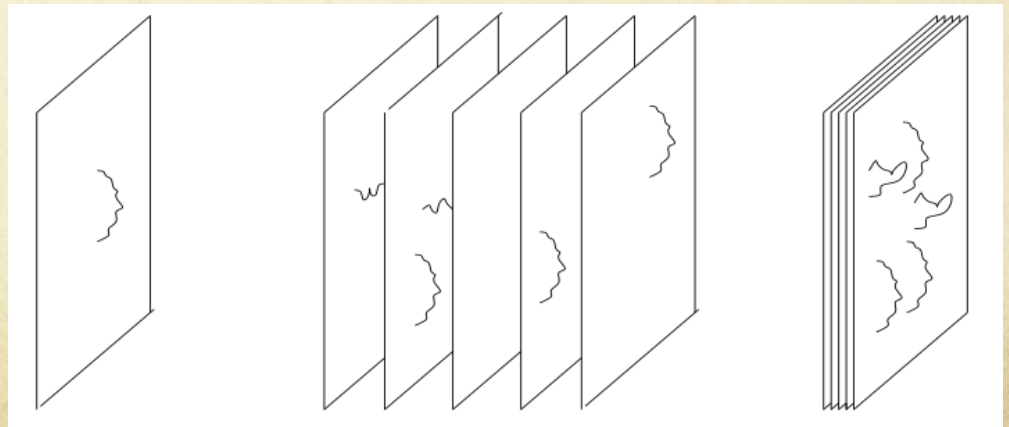
- D-branes are very special objects. They preserve half of the SUSYs

BPS states  $\rightarrow$  no force between parallel branes

- $D_p$ -branes couple to  $(p+1)$ -form potentials.
- Tension of  $D_p$ -brane:  $\tau_p^2 \propto g_s^{-2} \alpha'^{-(1-p)}$
- World-volume effective action of a single  $D_p$ -brane is  $(p+1)$ -dimensional Super Yang-Mills with gauge group  $U(1)$ .

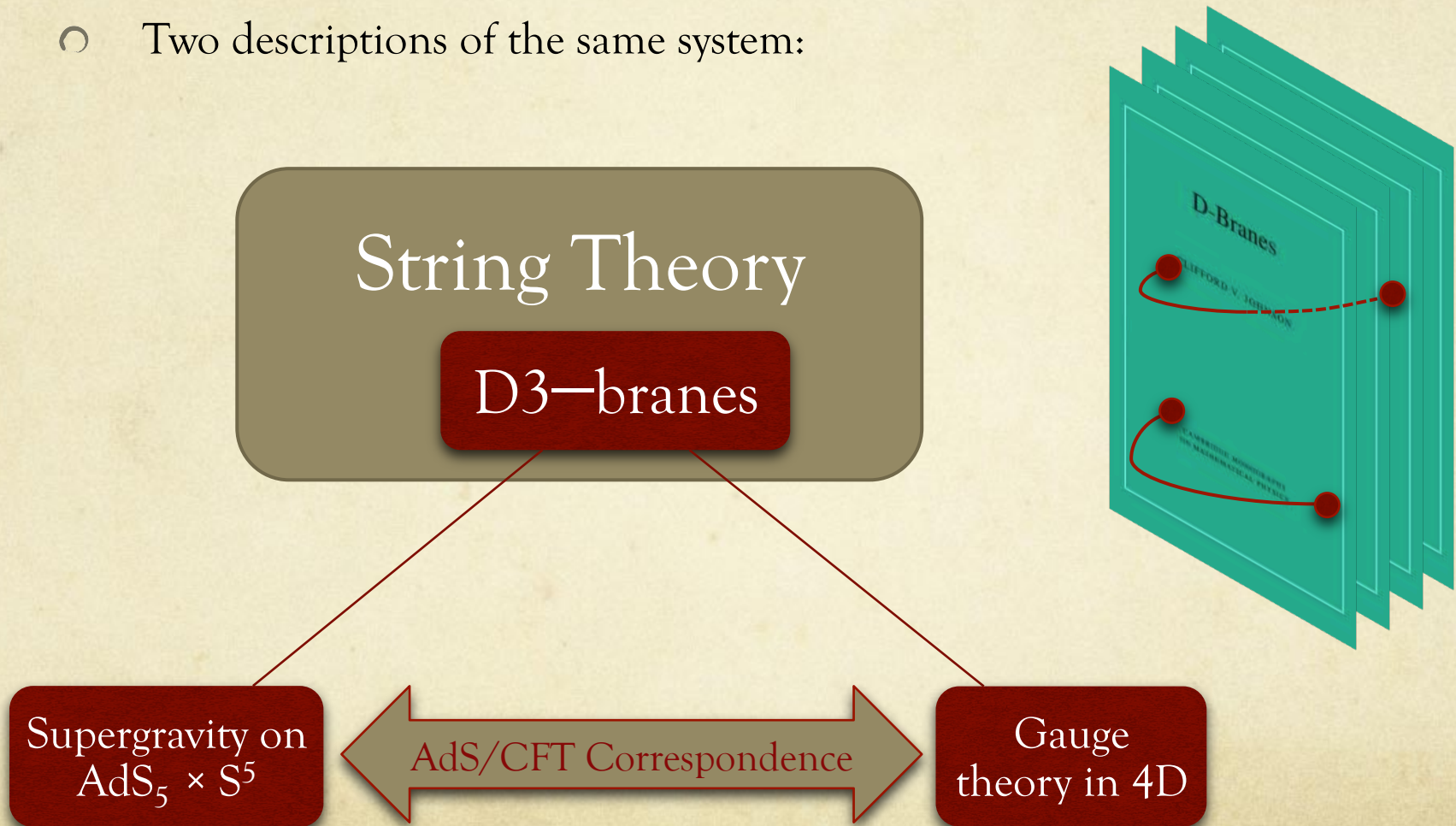
For  $N$  coincident branes there is symmetry enhancement:

$$U(1)^N \longrightarrow U(N)$$



# 'Deriving' the correspondence

- Consider type IIB superstring theory with a stack of  $N$  D3-branes.
- Two descriptions of the same system:



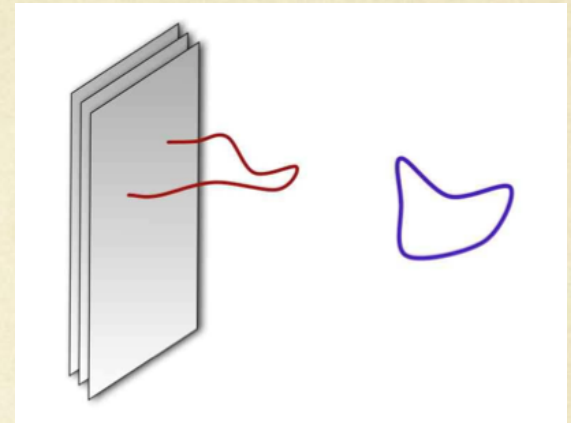


# Taking limits (cleverly)

- Can use  $N$  as a parameter, in addition to  $g_s$  and  $\alpha'$ .
- Weak coupling limit:  $g_s \rightarrow 0$ ,  $N$  fixed.

Back-reaction can be ignored and we just get

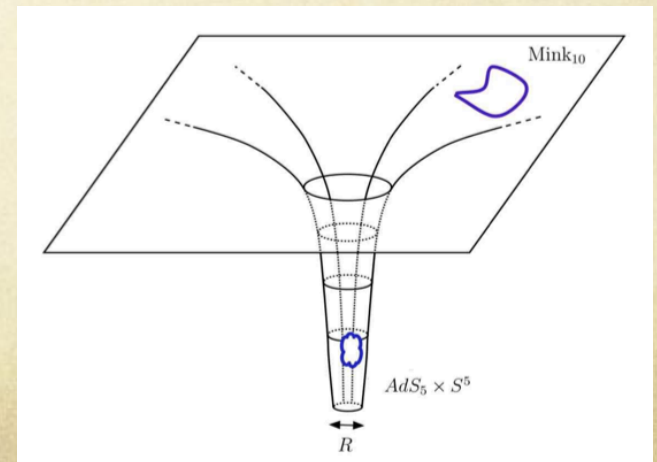
4d SYM with gauge group  $SU(N)$  'living on the branes'



- 't Hooft limit:  $g_s \rightarrow 0$ ,  $N \rightarrow \infty$ ,  $\lambda = g_s N$  fixed.

Back-reaction ( $\propto g_s N$ ) cannot be neglected.

D-branes source a classical supergravity solution.

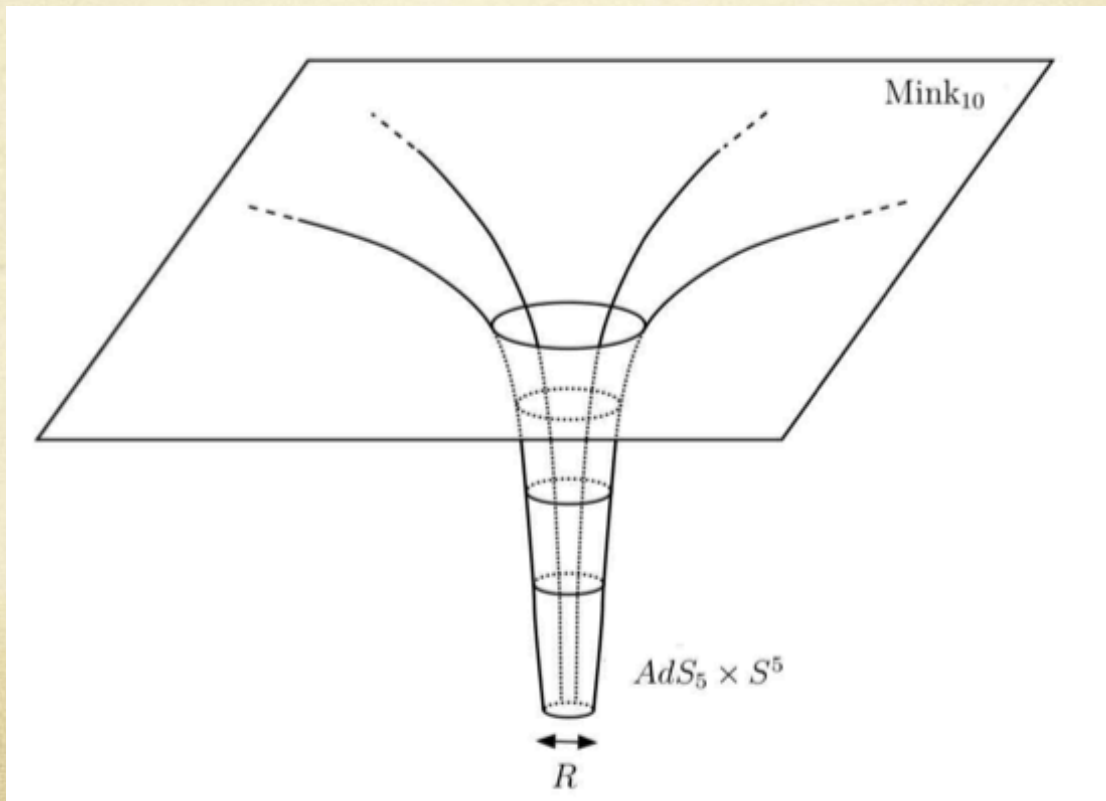


# Throat geometry

$$ds^2 = f^{-1/2}(-dt^2 + d\vec{x}^2) + f^{1/2}(dr^2 + r^2 d\Omega_5^2), \quad f = 1 + \frac{R^4}{r^4}, \quad R^4 = 4\pi g_s N \alpha'^2$$

○ For  $r \gg R$  we get flat spacetime.

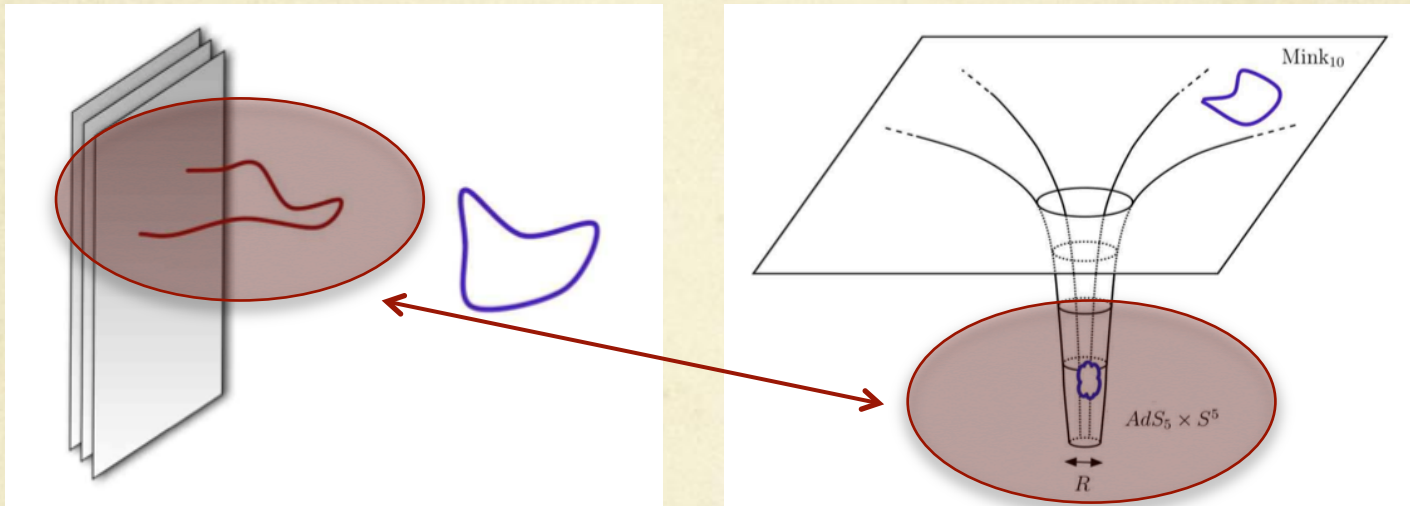
○ For  $r \ll R$  we get  $AdS_5 \times S^5$  geometry:  $ds^2 \approx \frac{R^2}{r^2} dr^2 + \frac{r^2}{R^2}(-dt^2 + d\vec{x}^2) + R^2 d\Omega_5^2$





# The decoupling limit

- For low energies,  $E \ll \alpha'$ , only massless modes can be excited.
- 10d supergravity describing the massless modes in the bulk and in the asymptotically flat region both decouple.



4d SU(N) SYM

with  $g_{\text{YM}}^2 = 2\pi g_s$



IIB string theory on AdS<sub>5</sub> × S<sup>5</sup>

with  $R^4 = 4\pi \lambda \alpha'^2$

# Strong/weak duality

$$\frac{R^4}{\alpha'^2} = 4\pi\lambda \quad \text{and} \quad g_s = \frac{\lambda}{2\pi N}$$

- $O(\alpha')$  corrections  $\longleftrightarrow$   $O(\lambda^{-1/2})$  corrections
- $O(g_s)$  corrections  $\longleftrightarrow$   $O(N^{-1})$  corrections (at fixed  $\lambda$ )

This is both a blessing and a curse!



# Matching of symmetries

- The  $\text{AdS}_d$  metric can be obtained from the embedding of a hyperboloid in  $(d+1)$ -dimensional flat spacetime ('with two time coordinates').

➔ the isometry group of  $\text{AdS}_d$  is  $\text{SO}(2, d-1)$

- The isometry group of  $S^5$  is  $\text{SO}(6)$ , the rotation group.

- The isometry group of  $\text{AdS}_5 \times S^5$  is  $\text{SO}(2, 4) \times \text{SO}(6)$ .

- This precisely matches the conformal symmetry and R-symmetry of SYM

(rotations of the six scalar fields)

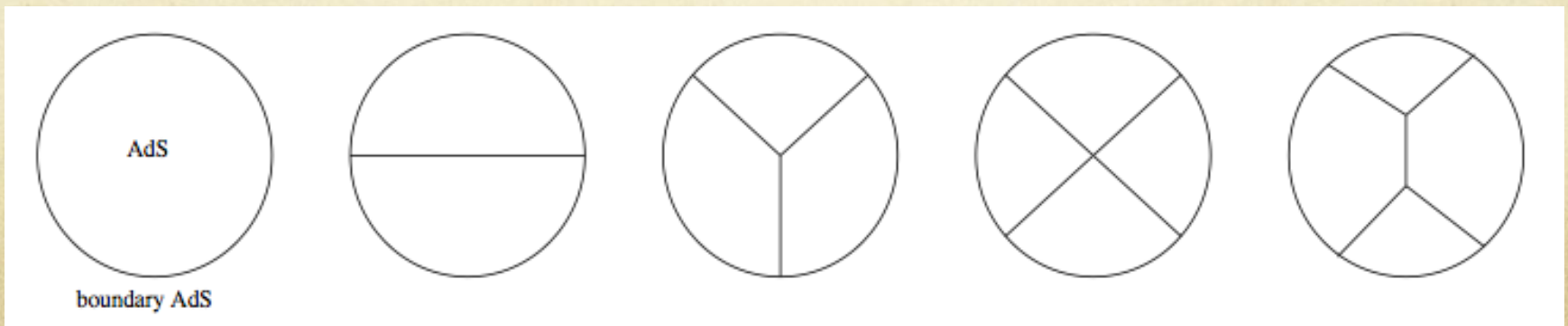
# AdS/CFT in practice

- The precise statement of the correspondence is the **equality of the partition functions of the two theories**:

$$\int_{\phi|_{\partial} = \bar{\phi}} D\phi(z, \vec{x}) e^{-S[\phi(z, \vec{x})]} \equiv Z_{AdS}[\bar{\phi}(\vec{x})] = Z_{CFT}[\bar{\phi}(\vec{x})] \equiv \left\langle e^{\int d^d x \bar{\phi}(\vec{x}) O(\vec{x})} \right\rangle$$

- Boundary conditions in AdS are associated with sources for the field operators.
- Computing correlators is straightforward:

$$\langle O_{\Delta_1}(x_1) O_{\Delta_2}(x_2) \dots \rangle = \left. \frac{\partial^n Z[\phi_{\Delta_i}]}{\partial \bar{\phi}_{\Delta_1}(x_1) \partial \bar{\phi}_{\Delta_2}(x_2) \dots} \right|_{\bar{\phi}_{\Delta_i}=0}$$





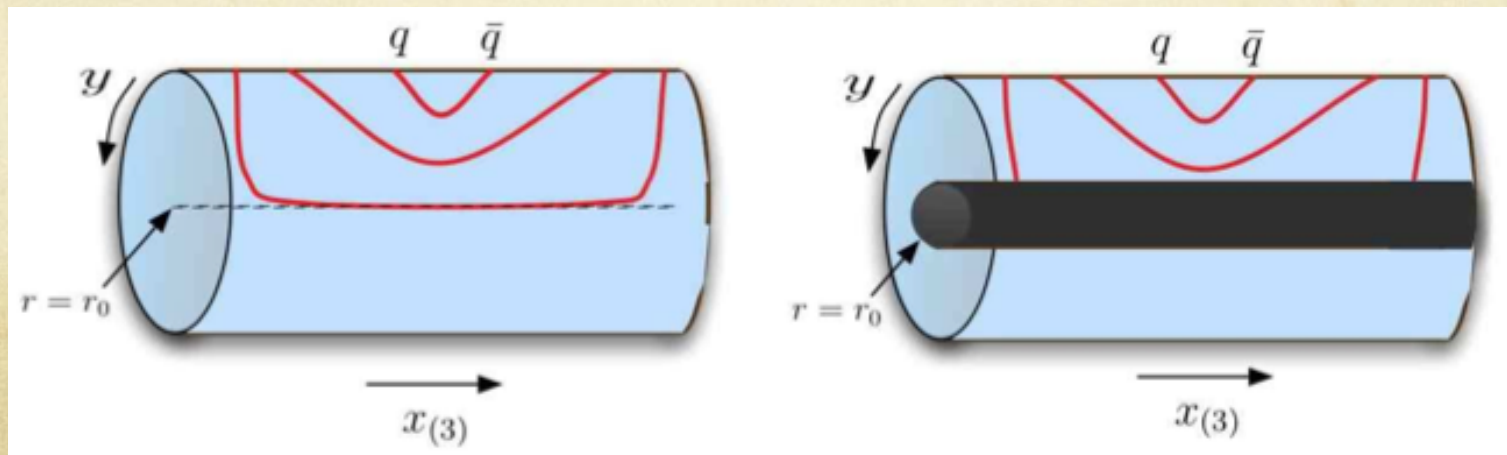
# Applications: modeling QCD

- 4d SYM is conformal but QCD is not. Actually they are very different theories:  
QCD is asymptotically free, exhibits confinement and is not SUSY.
- It is known how to construct gravitational duals for confining theories.

Confinement/deconfinement phase transition



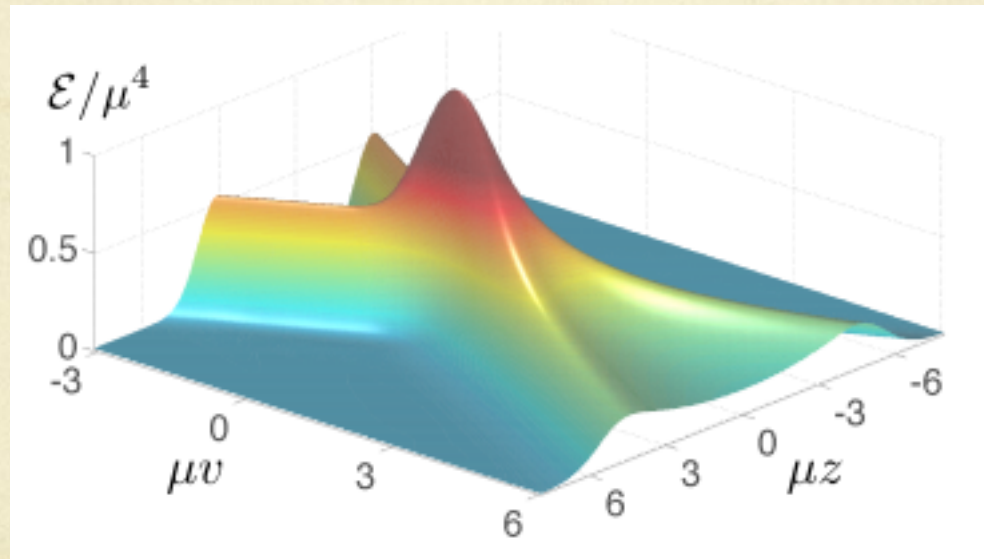
Hawking-Page phase transition



# Applications: Heavy ion collisions

- Transport coefficients (e.g. viscosity) can be computed from correlation functions.

AdS/CFT is a great tool to study quark-gluon plasmas (strongly coupled systems) that are observed at particle accelerators.





# Applications: Holographic superconductors

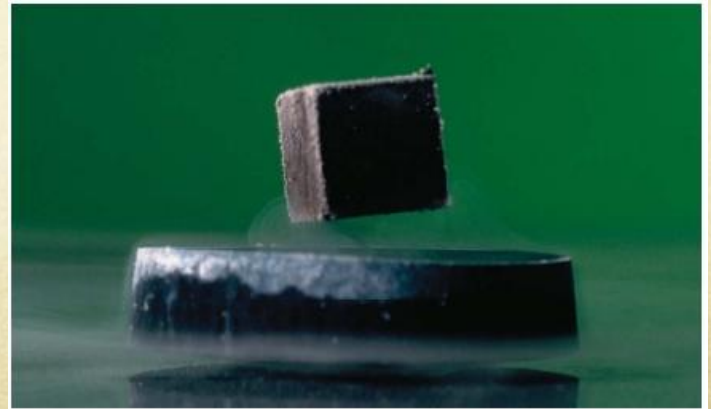
- We have a theory (BCS, 1957) that correctly describes low  $T_c$  superconductors.

Weakly coupled Cooper pairs of electrons form and condense below temperature  $T_c$ .

- But in 1986 a new class of high  $T_c$  superconductors was discovered!

These are not well understood: the electron pairing mechanism is strong coupling.

- AdS/CFT is appropriate to address this problem and holographic superconductors have been theoretically constructed with very similar qualitative properties as real world high  $T_c$  superconductors.



# Applications: Hydrodynamics and turbulence

- The fluid-gravity correspondence shows that the **Navier-Stokes equations can be obtained from the Einstein equations** (in the regime of long wavelength perturbations of AdS black holes).

- Can we understand turbulence?





# Conclusions

- Is String Theory the correct theory of quantum gravity?  
It is certainly an excellent candidate (arguably the best).
- We are perhaps still far from confirming the 'reality' of String Theory but it has already produced an extremely important legacy:

the AdS/CFT correspondence.

